

Properties of Triangles

Names of Triangles - Based on Angles

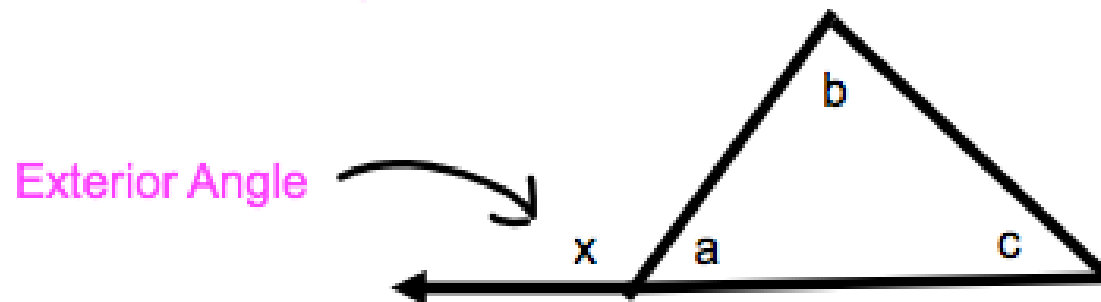
- 1) Acute: all angles are acute, less than 90°
- 2) Right: has one right angle, 90°
- 3) Obtuse: has one obtuse angle, larger than 90°

Names of Triangles - Based on Sides

- 1) Scalene: no congruent sides
- 2) Isosceles: 2 congruent sides
- 3) Equilateral: all congruent sides

Triangle Sum Property: all three angles must sum to 180° .

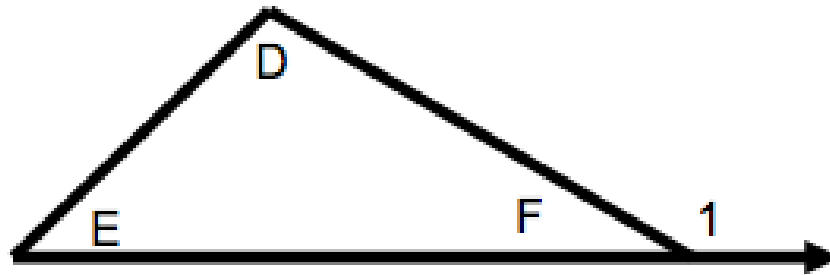
Exterior Angle: an angle that is adjacent to and supplementary to an interior angle of a triangle.
: the measure of the exterior angle of a triangle equals the sum of the remote interior angles.



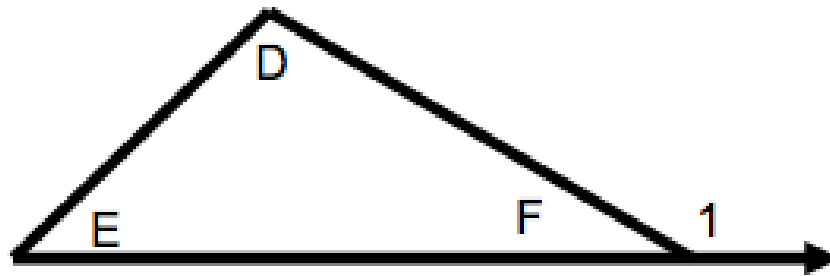
$$m\angle x = m\angle b + m\angle c$$

$$m\angle x + m\angle a = 180^\circ$$

1) The measurement of angle 1 is 150° . Angle D is twice that of Angle E.
Find the measurements of all three angles.



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If $\angle 1 = 150$, then
 $\angle F = 30$ because
supplementary angles.

$$\angle E = x$$

$$\angle D = 2x$$

$$2x + x + 30 = 180 \quad \triangle \text{ Sum Property}$$

$$3x = 150$$

$$x = 50$$

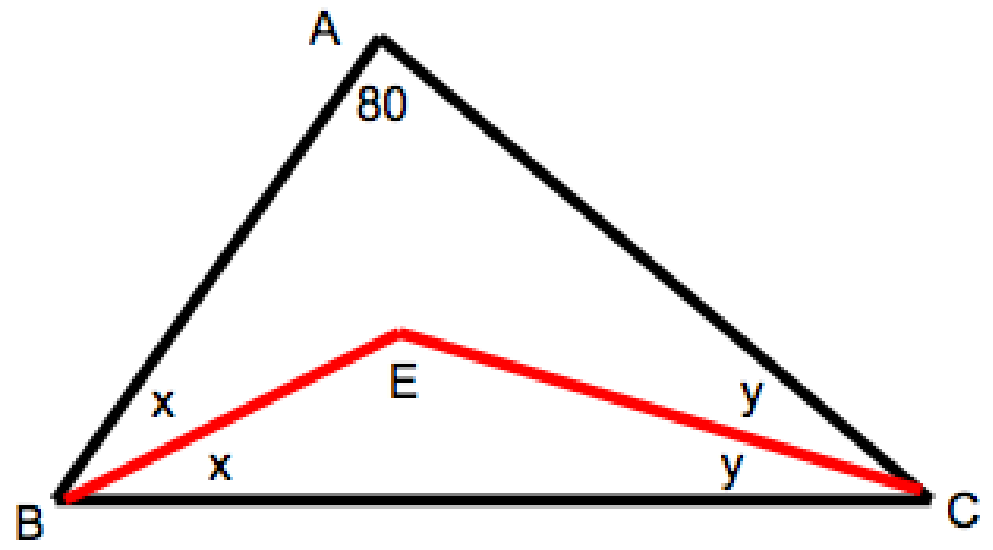
$$\angle D = 100^\circ$$

$$\angle E = 50^\circ$$

$$\angle F = 30^\circ$$

$$\underline{180^\circ} \checkmark$$

2) Find the measurement of Angle E.



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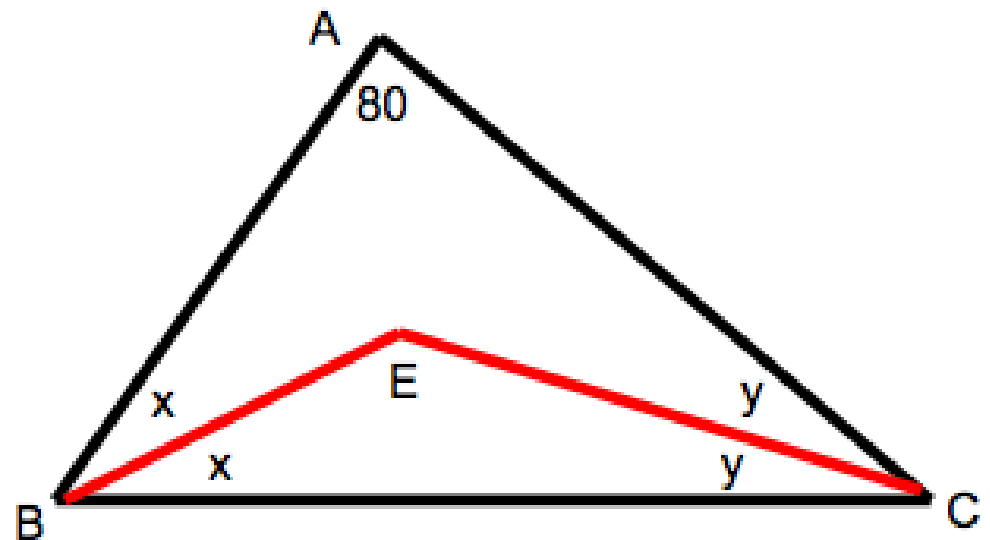
\triangle Sum Property $\triangle ABC$

$$2x + 2y + 80 = 180$$

$$2x + 2y = 100$$

reduce by 2

$$x + y = 50$$



Triangle Sum Property $\triangle BEC$

$$x + y + \angle E = 180$$

Substitute 50 for $x + y$

$$50 + \angle E = 180$$

$$\angle E = 130^\circ$$